Work & Energy – Q3 [5 marks](19/6/21)

Exam Boards

OCR : Mechanics (Year 1)

MEI: Mechanics a

AQA: Mechanics (Year 1)

Edx: Mechanics 1 (Year 1)

A car of mass 1200kg starts to descend a slope at $10ms^{-1}$. The slope is at a constant angle θ to the horizontal, where $sin\theta = \frac{1}{10}$. If the car is not accelerating or braking, and there is a constant resistance to motion of 500N, find the speed of the car when it has travelled 100m. Assume that $g = 10ms^{-2}$. [5 marks]

Solution

Method 1

By the Work-Energy principle,

Gain in KE = Work done by forces,

so that $\frac{1}{2}(1200)(v^2 - 10^2) = 1200g(100sin\theta) - 500(100)$ [3 marks] $\Rightarrow 600v^2 = 120000 - 50000 + 60000 = 130000$ $\Rightarrow v^2 = \frac{650}{3} \Rightarrow v = 14.7 \, ms^{-1} \, (3sf)$ [2 marks]

Method 2

By Conservation of Energy,

work done against resistance = loss of PE - gain in KE

$$\Rightarrow 500(100) = 1200g(100sin\theta) - \frac{1}{2}(1200)(v^2 - 10^2),$$

which gives the same equation.