

## **STEP Questions by Topic - Pure (25 pages; 14/7/23)**

For 2005 onwards (formulae booklet allowed up to 2018).

No STEP 1 for 2020 onwards.

\*  $\Rightarrow$  recommended; \*\*  $\Rightarrow$  highly recommended

### **Algebra**

#### **Paper 1**

2005, P1, Q3

2005, P1, Q7

2007, P1, Q4 (cubic)

2009, P1, Q3

2010, P1, Q1 (simultaneous eq'ns)

2013, P1, Q1

2014, P1, Q3

2019, P1, Q6

#### **Paper 3**

2008, P3, Q1

2009, P3, Q5 (simultaneous eq'ns)

2020, P3, Q5 (algebraic fractions)

### **Binomial Expansions**

#### **Paper 1**

2010, P1, Q5\*

2013, P1, Q6 (Fibonacci sequence)

## **Paper 2**

2007, P2, Q1\*

2016, P2, Q5

## **Paper 3**

2017, P3, Q1

## **Calculus**

### **Paper 1**

2008, P1, Q2

2011, P1, Q5

2014, P1, Q4\* (hands of clock)

2009, P1, Q5 (cone)

2016, P1, Q4 (curvature)

### **Paper 2**

2005, P2, Q1

### **Paper 3**

2007, P3, Q5

2009, P3, Q7

2015, P3, Q7 (operator D)

2017, P3, Q6

2019, P3, Q2

## Complex Numbers

These often boil down to geometry problems. The topic is easy to identify on the paper.

### Paper 2

2020, P2, Q7 (loci)

### Paper 3

2005, P3, Q8

2006, P3, Q5

2007, P3, Q6

2008, P3, Q7

2009, P3, Q6\*

2010, P3, Q3

2011, P3, Q3

2011, P3, Q8\*

2012, P3, Q6\*

2013, P3, Q4

2013, P3, Q6\*

2013, P3, Q8\*

2014, P3, Q5

2015, P3, Q6

2016, P3, Q7

2017, P3, Q2

2018, P3, Q6

2018, P3, Q7

2019, P3, Q6

2020, P3, Q3

## **Counting**

### **Paper 1**

2005, P1, Q1

2007, P1, Q1

2009, P1, Q1

## **Curves (not involving sketches)**

### **Paper 1**

2006, P1, Q6

2009, P1, Q2

2011, P1, Q1

2018, P1, Q1

### **Paper 2**

2008, P2, Q4

2009, P2, Q1

2009, P2, Q2

2010, P2, Q1 (osculating circle)

2010, P2, Q8

## **Paper 3**

2005, P3, Q5

## **Curve Sketching**

### **Paper 1**

2007, P1, Q8

2008, P1, Q6\*

2010, P1, Q2\*

2012, P1, Q2

2013, P1, Q5

2014, P1, Q2\* (ln)

2015, P1, Q1

2016, P1, Q3

2019, P1, Q2

### **Paper 2**

2005, P2, Q3

2006, P2, Q2

2006, P2, Q5

2007, P2, Q2\*

2008, P2, Q3 (cubic)

2009, P2, Q2

2011, P2, Q1\*

2011, P2, Q8

2012, P2, Q5

2013, P2, Q1\* ( $p^q$  &  $q^p$ )

2013, P2, Q4

2013, P2, Q5

2014, P2, Q7 (modulus function)

2015, P2, Q4

2016, P2, Q1

2017, P2, Q3

2020, P2, Q2 (differential eq'n)

### **Paper 3**

2005, P3, Q1

2005, P3, Q2

2006, P3, Q1

2007, P3, Q4 (radius of curvature)

2009, P3, Q3

2012, P3, Q3

2018, P3, Q1

2019, P3, Q7 ('Devil's curve')

2020, P3, Q2\* (hyperbolic functions)

2020, P3, Q6 (polar curves)

## Differential Equations

These questions usually follow a similar pattern, with each part providing inspiration for the next. The topic is easy to identify on the paper.

### Paper 1

2005, P1, Q8

2008, P1, Q8

2010, P1, Q6

2011, P1, Q7

2012, P1, Q8

2013, P1, Q7

### Paper 2

2005, P2, Q8

2007, P2, Q6\*

2008, P2, Q7\*

2014, P2, Q5

2016, P2, Q6

2018, P2, Q8

2019, P2, Q6

2020, P2, Q2 (sketching curves)

### Paper 3

2005, P3, Q2

2006, P3, Q7

2007, P3, Q8

2008, P3, Q6

2009, P3, Q2

2010, P3, Q7

2010, P3, Q8

2011, P3, Q1

2012, P3, Q1

2012, P3, Q7

2013, P3, Q7

2015, P3, Q8

2018, P3, Q3

2019, P3, Q1

2020, P3, Q7

## **Functions**

This topic is difficult to prepare for, as questions are of an (especially) one-off nature.

### **Paper 1**

2008, P1, Q4 (convex functions)

2008, P1, Q6\* (inverse functions)

2013, P1, Q2 (greatest integer less than or equal to  $x$ )

2013, P1, Q8 (composite functions)

2017, P1, Q6

## **Paper 2**

2007, P2, Q5 (composite functions)

2007, P2, Q7 (concave functions)

2008, P2, Q6 (periodic function)

2011, P2, Q3

2013, P2, Q8

2014, P2, Q7 (modulus function)

2013, P2, Q7

2018, P2, Q2 (concave function)

2018, P2, Q3 (rotational symmetry)

## **Paper 3**

2006, P3, Q4

2009, P3, Q3 (even function)

2009, P3, Q4 (Laplace transform)

2009, P3, Q7

2011, P3, Q4

2016, P3, Q8

2017, P3, Q4 (geometric mean)

## **Geometry**

This topic is difficult to prepare for, as questions are of an (especially) one-off nature.

## Paper 1

2005, P1, Q2

2005, P1, Q6

2006, P1, Q2\* (goat)

2006, P1, Q4 (polygon)

2006, P1, Q8 (tetrahedron)

2007, P1, Q5 (octahedron)

2008, P1, Q7

2009, P1, Q4

2009, P1, Q8 (incircle of triangle)

2010, P1, Q3

2011, P1, Q1

2011, P1, Q4

2012, P1, Q1

2012, P1, Q4

2014, P1, Q8

2015, P1, Q3

2015, P1, Q4

2016, P1, Q5

2017, P1, Q3

2017, P1, Q5

2017, P1, Q7

2018, P1, Q1

2018, P1, Q3

2019, P1, Q1

## **Paper 2**

2005, P2, Q5

2006, P2, Q7 (ellipse)

2010, P2, Q6 (tetrahedron)

2012, P2, Q6 (cyclic quadrilateral)

2014, P2, Q1

2014, P2, Q3

2015, P2, Q2

2015, P2, Q7

2017, P2, Q5

2020, P2, Q4 (triangles)

## **Paper 3**

2008, P3, Q3 (ellipse)

2009, P3, Q1 (circle)

2010, P3, Q5

2010, P3, Q6 (sphere)

2012, P3, Q5 (rational points)

2013, P3, Q8\*

2014, P3, Q3

2016, P3, Q2

2017, P3, Q7 (ellipse)

2018, P3, Q4 (hyperbola)

## **Hyperbolic functions**

### **Paper 3**

2005, P3, Q6 (see Erratum, included with paper)

2008, P3, Q4

2014, P3, Q6

2016, P3, Q4

2016, P3, Q6

2020, P3, Q2\*

## **Induction**

The topic is easy to identify on the paper, in that 'induction' will be mentioned.

### **Paper 1**

2017, P1, Q8

### **Paper 2**

2013, P2, Q6

2015, P2, Q3

2015, P2, Q5

2017, P2, Q6

### **Paper 3**

2005, P3, Q4

2007, P3, Q3

2008, P3, Q5

2011, P3, Q7

2018, P3, Q2

## **Inequalities**

### **Paper 1**

2008, P1, Q3

2012, P1, Q3

2014, P1, Q5

2017, P1, Q2

### **Paper 2**

2006, P2, Q6

2008, P2, Q5\*

2012, P2, Q4

2014, P2, Q2

2016, P2, Q4

2017, P2, Q4 (Schwarz inequality)

### **Paper 3**

2011, P3, Q4

2018, P3, Q5 (Arithmetic & Geometric means)

## **Integers**

### **Paper 1**

2006, P1, Q1

2007, P1, Q6

2009, P1, Q1

2010, P1, Q8

2011, P1, Q8

2014, P1, Q1

2015, P1, Q8

2016, P1, Q7

### **Paper 2**

2005, P2, Q2

2006, P2, Q3

2011, P2, Q2

2013, P2, Q7

2014, P2, Q8

2018, P2, Q6 (prime numbers)

2020, P2, Q5 (divisibility)

### **Paper 3**

2013, P3, Q5 (prime numbers)

2016, P3, Q5 (prime numbers)

## Integration

Integration questions have the advantage of being instantly recognisable.

### Paper 1

2005, P1, Q5

2006, P1, Q5

2006, P1, Q7

2007, P1, Q3

2008, P1, Q2

2008, P1, Q6\*

2009, P1, Q6

2009, P1, Q7

2010, P1, Q4

2011, P1, Q2\*

2012, P1, Q5\*

2013, P1, Q4

2014, P1, Q2

2015, P1, Q5

2016, P1, Q2

2017, P1, Q1

2018, P1, Q4

2018, P1, Q8

2019, P1, Q3\*

2019, P1, Q8

**Paper 2**

2005, P2, Q3

2006, P2, Q4

2007, P2, Q3

2007, P2, Q6

2008, P2, Q5\*

2009, P2, Q5

2009, P2, Q7

2010, P2, Q2

2010, P2, Q4\*

2011, P2, Q6\*

2012, P2, Q3\*

2013, P2, Q2

2014, P2, Q4\*

2015, P2, Q6

2016, P2, Q7\*

2017, P2, Q1

2017, P2, Q4

2018, P2, Q5

2019, P2, Q2\*

2020, P2, Q1\*

## **Paper 3**

2005, P3, Q7

2006, P3, Q2\*

2007, P3, Q7\*

2009, P3, Q8

2010, P3, Q2

2010, P3, Q8

2011, P3, Q6

2013, P3, Q1

2014, P3, Q2\*

2014, P3, Q4

2015, P3, Q1

2016, P3, Q1

2016, P3, Q3

2018, P3, Q8

2019, P3, Q5\* (see Erratum, provided with the paper)

2020, P3, Q1 (induction)

2021, P3, Q3\*\*

## **Irrational numbers**

### **Paper 1**

2008, P1, Q1

2019, P1, Q7

## **Paper 3**

2015, P3, Q5

## **Logarithms**

### **Paper 2**

2013, P2, Q1\* ( $p^q$  &  $q^p$ )

## **Matrices**

### **Paper 2**

2019, P2, Q8

2020, P2, Q6 (trace)

2021, P2, Q7\*

### **Paper 3**

2019, P3, Q3\* (time-consuming)

2020, P3, Q4

## **Polar Coordinates**

### **Paper 3**

2011, P3, Q5

2006, P3, Q6

2011, P3, Q5

2015, P3, Q3

2017, P3, Q5

2020, P3, Q6

## **Polynomials**

### **Paper 1**

2006, P1, Q3\* (quadratics & cubics)

2007, P1, Q4

2008, P1, Q5 (Chebyshev's theorem)

2012, P1, Q2

2015, P1, Q7

2016, P1, Q1

2018, P1, Q5

2018, P1, Q7\* (solving cubic eq'ns)

2019, P1, Q4

### **Paper 2**

2007, P2, Q2\*

2008, P2, Q3\* (cubic)

2009, P2, Q4

2010, P2, Q7 (cubic)

2012, P2, Q2

2013, P2, Q3 (cubic)

2016, P2, Q2

2016, P2, Q3 (truncated exponential function)

2018, P2, Q1 (quartic)

2019, P2, Q1\*

2019, P2, Q3

2020, P2, Q8 (quartic & quintic)

### **Paper 3**

2005, P3, Q3

2006, P3, Q8

2010, P3, Q4

2011, P3, Q2

2011, P3, Q3

2015, P3, Q4

2017, P3, Q3 (quartic)

2018, P3, Q1 (quadratic)

2019, P3, Q4 (reflexive polynomials)

### **Recurrence relations**

#### **Paper 1**

2006, P2, Q1

2012, P1, Q7

2014, P1, Q6

#### **Paper 2**

2008, P2, Q1 (sequence of points)

2012, P2, Q8

#### **Paper 3**

2005, P3, Q4

2008, P3, Q5

2008, P3, Q8

2012, P3, Q8

2018, P3, Q2

2020, P3, Q8

## **Sequences & Series**

This topic is difficult to prepare for, as questions are of an (especially) one-off nature.

### **Paper 1**

2011, P1, Q6

2016, P1, Q8 (generating functions)

2017, P1, Q4

2017, P1, Q8

### **Paper 2**

2005, P2, Q6\*

2008, P2, Q2

2009, P2, Q6 (Fibonacci)

2010, P2, Q3

2011, P2, Q7

2012, P2, Q1

2013, P2, Q6

2015, P2, Q1

2016, P2, Q8

2017, P2, Q2

2017, P2, Q6

2018, P2, Q5

2019, P2, Q4

2019, P2, Q5

2020, P2, Q3 (unimodal sequences)

### **Paper 3**

2007, P3, Q2

2008, P3, Q2

2008, P3, Q8

2010, P3, Q1

2012, P3, Q2

2012, P3, Q4

2013, P3, Q2 (Maclaurin Series)

2014, P3, Q1

2014, P3, Q8

2015, P3, Q2

2016, P3, Q4 (hyperbolic functions)

### **Trigonometry**

#### **Paper 1**

2005, P1, Q4

2005, P1, Q7

2007, P1, Q2

2007, P1, Q3 (Integration)

2010, P1, Q3

2011, P1, Q3

2012, P1, Q6

2018, P1, Q6

## **Paper 2**

2005, P2, Q4

2007, P2, Q4

2008, P2, Q6

2009, P2, Q3

2011, P2, Q4

2014, P2, Q6

2015, P2, Q2

2017, P2, Q3

2018, P2, Q4

## **Paper 3**

2005, P3, Q1

2006, P3, Q3

2007, P3, Q1

2017, P3, Q8

## **Vectors**

These can be time-consuming; especially when the information given has to be converted to a number of simultaneous equations.

### **Paper 1**

2007, P1, Q7

2010, P1, Q7

2013, P1, Q3

2014, P1, Q7

2015, P1, Q6

2016, P1, Q6

2019, P1, Q5

### **Paper 2**

2005, P2, Q7

2006, P2, Q8

2007, P2, Q8

2008, P2, Q8

2009, P2, Q8

2010, P2, Q5

2011, P2, Q5

2012, P2, Q7

2015, P2, Q8

2017, P2, Q8

2018, P2, Q7

2019, P2, Q7\* (long)

### **Paper 3**

2013, P3, Q3

2014, P3, Q7\* (cyclic quadrilateral)

2019, P3, Q8 (pyramid)