

# STEP Questions by Topic - Pure (28 pages; 7/6/25)

No STEP 1 for 2020 onwards.

\* ⇒ recommended; \*\* ⇒ highly recommended

## Algebra

### Paper 1

2005, P1, Q3

2005, P1, Q7

2007, P1, Q4 (cubic)

2009, P1, Q3

2010, P1, Q1 (simultaneous eq'ns)

2013, P1, Q1

2014, P1, Q3

2019, P1, Q6

### Paper 3

2008, P3, Q1

2009, P3, Q5 (simultaneous eq'ns)

2020, P3, Q5 (algebraic fractions)

## Binomial Expansions

### Paper 1

2010, P1, Q5\*

2013, P1, Q6 (Fibonacci sequence)

**Paper 2**

2007, P2, Q1\*

2016, P2, Q5

**Paper 3**

2017, P3, Q1

**Calculus**

**Paper 1**

2008, P1, Q2

2011, P1, Q5

2014, P1, Q4\* (hands of clock)

2009, P1, Q5 (cone)

2016, P1, Q4 (curvature)

**Paper 2**

2005, P2, Q1

**Paper 3**

2007, P3, Q5

2009, P3, Q7

2015, P3, Q7 (operator D)

2017, P3, Q6

2019, P3, Q2

## Complex Numbers

These often boil down to geometry problems. The topic is easy to identify on the paper.

### Paper 2

Specimen, P2, Q3

2020, P2, Q7 (loci)

### Paper 3

1987, P3, Q3

2005, P3, Q8

2006, P3, Q5

2007, P3, Q6

2008, P3, Q7

2009, P3, Q6\*

2010, P3, Q3

2011, P3, Q3

2011, P3, Q8\*

2012, P3, Q6\*

2013, P3, Q4

2013, P3, Q6\*

2013, P3, Q8\*

2014, P3, Q5

2015, P3, Q6

2016, P3, Q7

2017, P3, Q2

2018, P3, Q6

2018, P3, Q7

2019, P3, Q6

2020, P3, Q3

## Counting

### Paper 1

Specimen P1, Q5\* (number of zeros at the end of  $365!$ )

2005, P1, Q1\*

2007, P1, Q1

2009, P1, Q1

## Curves (not involving sketches)

### Paper 1

2006, P1, Q6

2009, P1, Q2

2011, P1, Q1

2018, P1, Q1

### Paper 2

2008, P2, Q4

2009, P2, Q1

2009, P2, Q2

2010, P2, Q1 (osculating circle)

2010, P2, Q8

### **Paper 3**

2003, P3, Q4\* (parametric form)

2005, P3, Q5

2024, P3, Q8\*

## **Curve Sketching**

### **Paper 1**

2007, P1, Q8

2008, P1, Q6\*

2010, P1, Q2\*

2012, P1, Q2

2013, P1, Q5

2014, P1, Q2\* ( $\ln$ )

2015, P1, Q1

2016, P1, Q3

2019, P1, Q2

### **Paper 2**

2003, P2, Q6 \* (modulus function)

2005, P2, Q3

2006, P2, Q2

2006, P2, Q5

2007, P2, Q2\*

2008, P2, Q3 (cubic)

2009, P2, Q2

2011, P2, Q1\*\* (square roots)

2011, P2, Q8

2012, P2, Q5

2013, P2, Q1\* ( $p^q$  &  $q^p$ )

2013, P2, Q4

2013, P2, Q5

2014, P2, Q7 (modulus function)

2015, P2, Q4

2016, P2, Q1

2017, P2, Q3

2020, P2, Q2 (differential eq'n)

### Paper 3

2005, P3, Q1

2005, P3, Q2

2006, P3, Q1

2007, P3, Q4 (radius of curvature)

2009, P3, Q3

2012, P3, Q3

2018, P3, Q1

2019, P3, Q7 ('Devil's curve')

2020, P3, Q2\* (hyperbolic functions)

(2020, P3, Q6) (polar curves)

## Differential Equations

These questions usually follow a similar pattern, with each part providing inspiration for the next. The topic is easy to identify on the paper.

### Paper 1

2005, P1, Q8

2008, P1, Q8

2010, P1, Q6

2011, P1, Q7

2012, P1, Q8

2013, P1, Q7

### Paper 2

2005, P2, Q8

2007, P2, Q6\*

2008, P2, Q7\*

2014, P2, Q5

2016, P2, Q6

2018, P2, Q8

2019, P2, Q6

2020, P2, Q2 (sketching curves)

### **Paper 3**

Specimen, P3, Q7\*

2005, P3, Q2

2006, P3, Q7

2007, P3, Q8

2008, P3, Q6

2009, P3, Q2

2010, P3, Q7

2010, P3, Q8

2011, P3, Q1

2012, P3, Q1

2012, P3, Q7

2013, P3, Q7

2015, P3, Q8

2018, P3, Q3

2019, P3, Q1

2020, P3, Q7

2024, P3, Q6\*\* (systems of equations)

### **Differentiation**

### **Paper 1**

Specimen, P1, Q2\*

## Digits

### Paper 1

2005, P1, Q1\*

## Functions

This topic is difficult to prepare for, as questions are of an (especially) one-off nature.

### Paper 1

2008, P1, Q4 (convex functions)

2008, P1, Q6\* (inverse functions)

2013, P1, Q2 (greatest integer less than or equal to  $x$ )

2013, P1, Q8 (composite functions)

2017, P1, Q6

### Paper 2

2003, P2, Q6\* (modulus function)

2007, P2, Q5 (composite functions)

2007, P2, Q7 (concave functions)

2008, P2, Q6 (periodic function)

2011, P2, Q3

2013, P2, Q8

2014, P2, Q7 (modulus function)

2013, P2, Q7

2018, P2, Q2 (concave function)

2018, P2, Q3 (rotational symmetry)

### **Paper 3**

2006, P3, Q4

2009, P3, Q3 (even function)

2009, P3, Q4 (Laplace transform)

2009, P3, Q7

2011, P3, Q4

2016, P3, Q8

2017, P3, Q4 (geometric mean)

## **Geometry**

This topic is difficult to prepare for, as questions are of an (especially) one-off nature.

### **Paper 1**

(Specimen, P1, Q8) (Coordinate Geometry)

(1988, P1, Q3) (Coordinate Geometry)

(1989, P1, Q6) (Coordinate Geometry)

(1990, P1, Q9) (Coordinate Geometry)

(1999, P1, Q2) (Coordinate Geometry)

(2004, P1, Q6) (Coordinate Geometry)

(2005, P1, Q2) (Coordinate Geometry)

(2005, P1, Q6) (Coordinate Geometry)

2006, P1, Q2\* (goat)

2006, P1, Q4 (polygon)

2006, P1, Q8 (tetrahedron)

2007, P1, Q5 (octahedron)

2008, P1, Q7

2009, P1, Q4

2009, P1, Q8 (incircle of triangle)

2010, P1, Q3

2011, P1, Q1

2011, P1, Q4

2012, P1, Q1

2012, P1, Q4

2014, P1, Q8

2015, P1, Q3

2015, P1, Q4

2016, P1, Q5

2017, P1, Q3

2017, P1, Q5

2017, P1, Q7

2018, P1, Q1

2018, P1, Q3

2019, P1, Q1

**Paper 2**

(1994, P2, Q7) (Coordinate Geometry)

2005, P2, Q5

2006, P2, Q7 (ellipse)

2010, P2, Q6 (tetrahedron)

2012, P2, Q6 (cyclic quadrilateral)

2014, P2, Q1

2014, P2, Q3

2015, P2, Q2

2015, P2, Q7

2017, P2, Q5

2020, P2, Q4 (triangles)

2023, P2, Q8\* (isosceles tetrahedron)

**Paper 3**

(1988, P3, Q8) (Coordinate Geometry)

(1989, P3, Q2) (Coordinate Geometry)

(1990, P3, Q2) (Coordinate Geometry)

(1991, P3, Q4) (Coordinate Geometry)

(1993, P3, Q8) (Coordinate Geometry)

(2001, P3, Q6) (Coordinate Geometry)

(2003, P3, Q7) (Coordinate Geometry)

(2005, P3, Q5) (Coordinate Geometry)

2008, P3, Q3 (ellipse)

2009, P3, Q1 (circle)

2010, P3, Q5

2010, P3, Q6 (sphere)

2012, P3, Q5 (rational points)

2013, P3, Q8\*

2014, P3, Q3

2016, P3, Q2

2017, P3, Q7 (ellipse)

2018, P3, Q4 (hyperbola)

## Hyperbolic functions

### Paper 2

Specimen, P2, Q4\*

### Paper 3

2005, P3, Q6 (see Erratum, included with paper)

2008, P3, Q4

2014, P3, Q6

2016, P3, Q4

2016, P3, Q6

2020, P3, Q2\*

## Induction

The topic is easy to identify on the paper, in that 'induction' will be mentioned.

### **Paper 1**

2017, P1, Q8

### **Paper 2**

2013, P2, Q6

2015, P2, Q3

2015, P2, Q5

2017, P2, Q6

### **Paper 3**

2005, P3, Q4

2007, P3, Q3

2008, P3, Q5

2011, P3, Q7

2018, P3, Q2

## **Inequalities**

### **Paper 1**

Specimen, P1, Q9

2008, P1, Q3

2012, P1, Q3

2014, P1, Q5

2017, P1, Q2

## Paper 2

2006, P2, Q6

2008, P2, Q5\*

2012, P2, Q4

2014, P2, Q2

2016, P2, Q4

2017, P2, Q4 (Schwarz inequality)

2020, P2, Q4\* (triangles)

## Paper 3

1987, P3, Q3\* (1<sup>st</sup> part)

2011, P3, Q4

2018, P3, Q5 (Arithmetic & Geometric means)

## Integers

### Paper 1

2006, P1, Q1

2007, P1, Q6

2009, P1, Q1

2010, P1, Q8

2011, P1, Q8

2014, P1, Q1

2015, P1, Q8

2016, P1, Q7

## Paper 2

2005, P2, Q2

2006, P2, Q3

2011, P2, Q2

2013, P2, Q7

2014, P2, Q8

2018, P2, Q6 (prime numbers)

2020, P2, Q5 (divisibility)

## Paper 3

2013, P3, Q5 (prime numbers)

2016, P3, Q5 (prime numbers)

## Integration

Integration questions have the advantage of being instantly recognisable.

## Paper 1

Specimen, P1, Q4\*

1987, P1, Q5\* (substitution)

1987, P1, Q8\* (substitution)

2005, P1, Q5\*

2006, P1, Q5

2006, P1, Q7

2007, P1, Q3\*

2008, P1, Q2

2008, P1, Q6\*

2009, P1, Q6

2009, P1, Q7

2010, P1, Q4

2011, P1, Q2\*

2012, P1, Q5\*

2013, P1, Q4

2014, P1, Q2

2015, P1, Q5

2016, P1, Q2

2017, P1, Q1

2018, P1, Q4

2018, P1, Q8

2019, P1, Q3\*

2019, P1, Q8

## Paper 2

Specimen, P2, Q7 (floor function; unusually short solution)

1987, P2, Q6\*\* (trigonometry)

2005, P2, Q3

2006, P2, Q4\*

2007, P2, Q3\*

2007, P2, Q6

2008, P2, Q5\*

2009, P2, Q5

2009, P2, Q7

2010, P2, Q2

2010, P2, Q4\*\*

2011, P2, Q6\*

2012, P2, Q3\*

2013, P2, Q2

2014, P2, Q4\*

2015, P2, Q6

2016, P2, Q7\*

2017, P2, Q1

2017, P2, Q4

2018, P2, Q5

2019, P2, Q2\*

2020, P2, Q1\*

2023, P2, Q1\*\*

### **Paper 3**

2005, P3, Q7

(2006, P3, Q2\*)

2007, P3, Q7\*

2009, P3, Q8

2010, P3, Q2

2010, P3, Q8

2011, P3, Q6

2013, P3, Q1

2014, P3, Q2\*

2014, P3, Q4

2015, P3, Q1

2016, P3, Q1

2016, P3, Q3

2018, P3, Q8

2019, P3, Q5\* (see Erratum, provided with the paper)

2020, P3, Q1 (induction)

2021, P3, Q3\*

2022, P3, Q5\*

## Irrational numbers

### Paper 1

2008, P1, Q1

2019, P1, Q7

### Paper 3

2015, P3, Q5

## Logarithms

### Paper 1

1987, P1, Q4\*\*

2018, P1, Q2\*\* (change of base)

### Paper 2

2013, P2, Q1\* ( $p^q$  &  $q^p$ )

## Matrices

### Paper 2

2019, P2, Q8

2020, P2, Q6 (trace)

2021, P2, Q7\*

### Paper 3

2019, P3, Q3\* (time-consuming)

2020, P3, Q4

2024, P3, Q5 (trace)

**Logic** [Hasn't appeared in STEP in recent years.]

### Paper 2

Specimen, P2, Q10 [True/False statements]

**Numbers****Paper 2**

2020, P2, Q5\*\* (divisibility)

**Polar Curves****Paper 3**

1989, P3, Q6\*\* (conics & lines)

(2006, P3, Q6) (parabola)

2011, P3, Q5

(2015, P3, Q3) (Conchoid of Nicomedes)

(2017, P3, Q5)

(2020, P3, Q6)

**Polynomials****Paper 1**

2006, P1, Q3\* (quadratics & cubics)

2007, P1, Q4

2008, P1, Q5 (Chebyshev's theorem)

2012, P1, Q2

2015, P1, Q7

2016, P1, Q1

2018, P1, Q5

2018, P1, Q7\* (solving cubic eq'ns)

2019, P1, Q4

## Paper 2

2007, P2, Q2\*

2008, P2, Q3\* (cubic)

2009, P2, Q4

2010, P2, Q7 (cubic)

2012, P2, Q2

2013, P2, Q3 (cubic)

2016, P2, Q2

2016, P2, Q3 (truncated exponential function)

2018, P2, Q1 (quartic)

2019, P2, Q1\*

2019, P2, Q3\* (integer roots)

2020, P2, Q8 (quartic & quintic)

## Paper 3

2005, P3, Q3

2006, P3, Q8

2010, P3, Q4

2011, P3, Q2

2011, P3, Q3

2015, P3, Q4

2017, P3, Q3 (quartic)

2018, P3, Q1 (quadratic)

2019, P3, Q4 (reflexive polynomials)

## Proof

### Paper 1

2005, P1, Q3

2006, P1, Q3\* (quadratic)

### Paper 2

2007, P2, Q4\*

## Recurrence relations

### Paper 1

2006, P2, Q1

2012, P1, Q7

2014, P1, Q6

### Paper 2

2008, P2, Q1 (sequence of points)

2012, P2, Q8

### Paper 3

2005, P3, Q4

2008, P3, Q5

2008, P3, Q8

2012, P3, Q8

2018, P3, Q2

2020, P3, Q8

## **Sequences & Series**

This topic is difficult to prepare for, as questions are of an (especially) one-off nature.

### **Paper 1**

2011, P1, Q6

2016, P1, Q8 (generating functions)

2017, P1, Q4

2017, P1, Q8

### **Paper 2**

2005, P2, Q6\*

2008, P2, Q2

2009, P2, Q6 (Fibonacci)

2010, P2, Q3

2011, P2, Q7

2012, P2, Q1

2013, P2, Q6

2015, P2, Q1

2016, P2, Q8

2017, P2, Q2

2017, P2, Q6

2018, P2, Q5

2019, P2, Q4

2019, P2, Q5

2020, P2, Q3 (unimodal sequences)

### **Paper 3**

1989, P3, Q9\*\*

2007, P3, Q2

2008, P3, Q2

2008, P3, Q8

2010, P3, Q1

2012, P3, Q2

2012, P3, Q4

2013, P3, Q2\* (Maclaurin Series)

2014, P3, Q1

2014, P3, Q8

2015, P3, Q2

2016, P3, Q4 (hyperbolic functions)

## **Trigonometry**

### **Paper 1**

2005, P1, Q4

2005, P1, Q7

2007, P1, Q2

2007, P1, Q3 (Integration)

2010, P1, Q3

2011, P1, Q3

2012, P1, Q6

2018, P1, Q6

## **Paper 2**

2005, P2, Q4

2007, P2, Q4

2008, P2, Q6

2009, P2, Q3

2011, P2, Q4

2014, P2, Q6

2015, P2, Q2

2017, P2, Q3

2018, P2, Q4

## **Paper 3**

2005, P3, Q1

2006, P3, Q3

2007, P3, Q1

2017, P3, Q8

## **Vectors**

These can be time-consuming; especially when the information given has to be converted to a number of simultaneous equations.

### **Paper 1**

2007, P1, Q7

2010, P1, Q7

2013, P1, Q3

2014, P1, Q7

2015, P1, Q6

2016, P1, Q6

2019, P1, Q5

### **Paper 2**

Specimen, P2, Q9\*

2005, P2, Q7

2006, P2, Q8

2007, P2, Q8

2008, P2, Q8

2009, P2, Q8

2010, P2, Q5

2011, P2, Q5

2012, P2, Q7

2015, P2, Q8

2017, P2, Q8

2018, P2, Q7

2019, P2, Q7\* (long)

2023, P2, Q8\* (isosceles tetrahedron)

### Paper 3

2013, P3, Q3

2014, P3, Q7\* (cyclic quadrilateral)

2019, P3, Q8 (pyramid)

2022, P3, Q7\* (vector triple product)