Minimum Connector - Q1 [Practice/E](16/6/21)

For the network below:

(i) Apply Kruskal's algorithm to create a minimum spanning tree (showing the order in which arcs are added), and giving the total weight.
(ii) Apply Prim's algorithm to create a minimum spanning tree starting at A (showing the order in which nodes are added), and giving the total weight.
(iii) Create a distance matrix for the network.
(iv) Use this matrix to apply Prim's algorithm - starting at J this time.

Solution
(i) $\mathrm{FI}(2) \mathrm{FG}(3) \mathrm{IE}(3) \mathrm{BE}(3) \mathrm{IH}(3) \mathrm{CD}(4) \mathrm{IJ}(5) \mathrm{AB}(5)$
[reject $\mathrm{FH}(5) \& \mathrm{GH}(5)] \mathrm{ED}(6)$ [spanning tree is complete]
Total weight: 34
(ii) $\mathrm{AB}(5) \mathrm{BE}(5) \mathrm{ED}(6) \mathrm{EI}(3) \mathrm{IF}(2) \mathrm{IH}(3) \mathrm{FG}(3) \mathrm{DC}(4)$

Total weight: 34
(iii) \& (iv)

|  | 10 | 6 | 9 | 8 | 5 | 3 | 4 | 7 | 2 | 1 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  | A | B | C | D | E | F | G | H | I | J |
| A |  | (5) |  |  | 9 | 10 | 12 |  |  |  |
| B | 5 |  | 7 | 8 | $(3)$ |  |  |  |  |  |
| C |  | 7 |  | $(4)$ |  |  |  |  |  |  |
| D |  | 8 | 4 |  | (6) |  |  |  |  |  |
| E | 9 | 3 |  | 6 |  |  |  |  | $(3)$ |  |
| F | 10 |  |  |  |  |  | 3 | 5 | $(2)$ |  |
| G | 12 |  |  |  |  | $(3)$ |  | 5 |  |  |
| H |  |  |  |  |  | 5 | 5 |  | $(3)$ |  |
| I |  |  |  |  | 3 | 2 |  | 3 |  | $(5)$ |
| J |  |  |  | 7 |  |  |  |  | 5 |  |

$\mathrm{JI}(5) \mathrm{IF}(2) \mathrm{FG}(3) \mathrm{IE}(3) \mathrm{EB}(3) \mathrm{IH}(3) \mathrm{ED}(6) \mathrm{DC}(4) \mathrm{BA}(5)$
Total weight: 34

