MAT: Specimen 2 - Q4 (2 Pages; 21/10/20)

(i)



(ii) Referring to the diagram in (i), as PX = RX,

PX + XQ = RX + XQ, and this is minimised when X lies on the line RQ.

In that case,
$$RX + XQ = RQ = \sqrt{(11 - 7)^2 + (2 - [-1])^2}$$

= $\sqrt{16 + 9} = 5$

(iii) See the diagram in (i).

(iv) Referring to the diagram below, ZQ = ZS, and so

$$PY + YZ + ZQ = PY + YZ + ZS$$

Also, as before, PY = RY,

so that PY + YZ + ZS = RY + YZ + ZS,

and this minimised when Y and Z lie on the line RS.

In that case, $PY + YZ + ZQ = RS = \sqrt{(2-7)^2 + (11 - [-1])^2}$ = $\sqrt{25 + 144} = 13$

