MAT Exercises - Differentiation - Sol'ns

(1) If
$$f(x) = x^2$$
, what is $f'(3x)$?

Solution

Method 1

Note that the differentiation is wrt 3x (rather than x).

Let
$$u = 3x$$
. Then $f'(3x) = f'(u) = \frac{d}{du}(u^2) = 2u = 2(3x) = 6x$

Method 2

$$f'(x) = 2x \Rightarrow f'(3x) = 2(3x) = 6x$$