## Proof - Q5 [Problem/E](4/10/21)

Suppose that a half price offer applies at selected stores of a supermarket for customers with loyalty cards.
$H$ is "Half price offer applies"
$S$ is "Customer shops at a selected store"
$L$ is "Customer has a loyalty card"
Place the following statements into equivalent groups. Which ones are true?
$H \Rightarrow S$
$H \Leftarrow S$
" $H$ is a necessary condition for $S$ "
" $S$ is a necessary condition for $H$ "
" $H$ is a sufficient condition for $S$ "
" $S$ is a sufficient condition for $H$ "
" $H$ is only true if $S$ is true"
" $S$ is only true if $H$ is true"

## Solution

$H \Rightarrow S$ (true)
" $S$ is a necessary condition for $H$ "
" $H$ is a sufficient condition for $S$ "
" $H$ is only true if $S$ is true"
$H \Leftarrow S$ (false)
" $H$ is a necessary condition for $S$ "
" $S$ is a sufficient condition for $H$ "
" $S$ is only true if $H$ is true"

