## Matrices – Q3 [Practice/M](26/5/21)

Use matrices to find the plane containing the points (2, -1, 4), (-3, 4, 2) and (1, 0, 5) (without using a calculator)

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## Solution

Let the eq'n of the plane be ax + by + cz = 1Then 2a - b + 4c = 1 (1) -3a + 4b + 2c = 1 (2) a + 5c = 1 (3) Thus  $\begin{pmatrix} 2 & -1 & 4 \\ -3 & 4 & 2 \\ 1 & 0 & 5 \end{pmatrix} \begin{pmatrix} a \\ b \\ c \end{pmatrix} = \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix}$   $\begin{vmatrix} 2 & -1 & 4 \\ -3 & 4 & 2 \\ 1 & 0 & 5 \end{vmatrix} = 2(20) - (-3)(-5) + (-18) = 7$   $\begin{pmatrix} 2 & -1 & 4 \\ -3 & 4 & 2 \\ 1 & 0 & 5 \end{vmatrix} = 2(20) - (-3)(-5) + (-18) = 7$   $\begin{pmatrix} 2 & -1 & 4 \\ -3 & 4 & 2 \\ 1 & 0 & 5 \end{pmatrix}^{-1} = \frac{1}{7} \begin{pmatrix} 20 & 17 & -4 \\ 5 & 6 & -1 \\ -18 & -16 & 5 \end{pmatrix}^{T}$ So  $\begin{pmatrix} a \\ b \\ c \end{pmatrix} = \frac{1}{7} \begin{pmatrix} 20 & 5 & -18 \\ 17 & 6 & -16 \\ 4 & 1 & 5 \end{pmatrix} \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix}$ ,

and hence  $a = \frac{1}{7}(20 + 5 - 18) = 1$ ,  $b = \frac{1}{7}(17 + 6 - 16) = 1$ ,  $c = \frac{1}{7}(-4 - 1 + 5) = 0$ and so the eq'n of the plane is x + y = 1