

Inequalities - Exercises (1 page; 7/10/18)

(1) How would you solve the inequality: $\frac{1}{x} < x$?

(2) Is $\frac{6}{7} < \frac{2}{\sqrt{5}}$?

(3) Which is larger: $\frac{\sqrt{7}}{2}$ or $\frac{1+\sqrt{6}}{3}$ (without using a calculator)?

(4) Show that $e^3 > 4e^{\frac{3}{2}}$

(5) Are the following true or false?

(i) $a < b \Rightarrow \frac{1}{a} > \frac{1}{b}$

(ii) $a < b \Rightarrow a^2 < b^2$

(iii) $a < b \ \& \ c < d \Rightarrow a + c < b + d$

(iv) $a < b \ \& \ c < d \Rightarrow a - c < b - d$

(6) Prove or provide a counter-example for the conjecture

$x > a \ \& \ y > b \Rightarrow xy > ab$ (a, b real) in each of the following cases:

(i) $a > 0, b > 0$ (ii) $a < 0, b < 0$ (iii) $a > 0, b < 0$

(7) Prove that $a + b < 1 + ab$ if $a > 1$ and $b > 1$