

Hyperbolic Functions – Q3 [Practice/E](17/6/23)

If $x = \sinh u$, write $\sinh(4u)$ in terms of x

Solution

$$\begin{aligned}\sinh(4u) &= 2 \sinh(2u) \cosh(2u) \\&= 4 \sinh u \cosh u (\cosh^2 u + \sinh^2 u) \\&= 4x\sqrt{1+x^2}(1+2x^2)\end{aligned}$$