## Curve Sketching - Exercises (2 pages; 12/8/19)

(1) Sketch the graph of 
$$\sqrt{x^2 - 2x + 1}$$
 for  $0 \le x \le 2$ 

- (2) (i) What possible shapes might a cubic have (ignoring its position relative to the axes)?
- (ii) How many stationary points does the cubic function,

$$f(x) = x^3 + x^2 - 2x + 3$$
 have?

- (iii) What is the condition for there to be 2 stationary points for the general cubic  $f(x) = ax^3 + bx^2 + cx + d$ ?
- (iv) For  $f(x) = ax^3 + bx^2 + cx + d$ , find the *x*-coordinate of any turning points of the gradient.

If the cubic has turning points, how could they be used to find the point of inflexion?

(v) For  $f(x) = ax^3 + bx^2 + cx + d$ , find conditions for the shape of the curve to be each of the 3 possibilities shown in (i), by considering the gradient at the point of inflexion.

(3) Sketch 
$$y = |x - 2| + 1$$

- (4)(i) Sketch the curve  $y = \frac{4x^2 + 5x + 7}{2x + 3}$ .
  - (ii) Without using calculus, find the coordinates of the stationary points (to 3sf).

- (5)(i) Find a series of transformations that can be applied to  $y = \frac{1}{x}$  to produce  $y = \frac{3x-2}{6x-1}$ .
- (ii) Hence or otherwise, sketch the curve  $y = \frac{3x-2}{6x-1}$ .