Complex Numbers Q19 - Practice/Y1/M (22/5/21)

How are the complex numbers $\cos \theta+i \sin \theta$ and $\sin \theta+i \cos \theta$ related?

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$$
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$$

Solution

$$
\sin \theta+i \cos \theta=\cos \left(\frac{\pi}{2}-\theta\right)+i \sin \left(\frac{\pi}{2}-\theta\right)
$$

As both complex numbers have a modulus of $1, \sin \theta+i \cos \theta$ is the reflection of $\cos \theta+i \sin \theta$ in the line $\mathrm{Re}=\operatorname{Im}$ (see diagram below).


