Complex Numbers Q14- Practice/Y1/E (22/5/21)
(i) How are the complex numbers $z$ and $z i$ related to each other geometrically?
(ii) How are the complex numbers $z$ and $\frac{1}{z}$ related to each other geometrically?
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## Solution

(i) $|i|=1 \& \arg (i)=\frac{\pi}{2}$; hence multiplication by $i$ has the effect of rotating $z$ by $\frac{\pi}{2}$ anti-clockwise.
(ii) $\left|\frac{1}{z}\right|=\frac{1}{|z|}$ and $\arg \left(\frac{1}{z}\right)=\arg (1)-\arg (z)=-\arg (z)$

So $\frac{1}{z}$ is obtained from $z$ by reflecting in the Real axis (ie obtaining $\left.z^{*}\right)$, and taking the reciprocal of the modulus of $z$

