

STEP/Integration Q4 (21/6/23)

$$\int \sqrt{1-x^2} dx$$

Solution

(speculative substitution)

Let $x = \sin\theta$, so that $dx = \cos\theta d\theta$

Then $\int \sqrt{1-x^2} dx = \int \cos\theta \cos\theta d\theta = \frac{1}{2} \int 1 + \cos 2\theta d\theta$ etc