

STEP/Differentiation Q4 (15/6/23)

Find $\frac{d}{dx}(x^{\sin x})$

Solution

$$\begin{aligned}\frac{d}{dx}(x^{\sin x}) &= \frac{d}{dx}(e^{\ln x \cdot \sin x}) = e^{\ln x \cdot \sin x} \left(\frac{1}{x} \sin x + \ln x \cdot \cos x \right) \\ &= x^{\sin x} \left(\frac{1}{x} \sin x + \ln x \cdot \cos x \right)\end{aligned}$$