Numerical Methods - Calculator method (1 page; 5/10/20)

Example: Finding $\sqrt{2}$ by an iterative method

Let (eg) $x_0 = 1.5$ be the first estimate for $\sqrt{2}$

Consider the rectangle with sides x_0 and $\frac{2}{x_0}$

As $x_0 \cdot \frac{2}{x_0} = 2$, one of these sides must be less than $\sqrt{2}$, and the other one greater.

The average of x_0 and $\frac{2}{x_0}$ will then be the next estimate, x_1

ie $x_1 = \frac{1}{2} (x_0 + \frac{2}{x_0})$

and so on, with $x_{r+1} = \frac{1}{2} (x_r + \frac{2}{x_r})$

On a calculator, try the following (it should work for Casio models):

1.5 = $0.5(Ans + 2 \div Ans)$ = [repeatedly]

You should get the sequence:

1.416666667 1.414215686 1.414213562 1.414213562