Graphs - Q5 [Practice/M] (25/5/21)

What combination of transformations converts $y = 2^x$ to $y = 2^{4x-2}$?

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Solution

 $y = 2^x \rightarrow y = 2^{4x}$ is a stretch of scale factor $\frac{1}{4}$ in the *x*-direction

Then
$$y = 2^{4x} \rightarrow y = 2^{4(x-\frac{1}{2})} = 2^{4x-2}$$
 is a translation of $\begin{pmatrix} \frac{1}{2} \\ 0 \end{pmatrix}$

[Alternatively, $y=2^{4x}\to y=\left(\frac{1}{4}\right)2^{4x}=2^{4x-2}$ is a stretch of scale factor $\frac{1}{4}$ in the y-direction.]