

Discrete Random Variables - Overview (9/6/21)

Q1 [8 marks]

The probability distribution of a discrete random variable is shown below.

x	1	2	3
$P(X = x)$	p	q	r

Given that $E(X) = \frac{7}{3}$ and $Var(X) = \frac{5}{9}$, find p, q and r .

Q2 [Practice/E]

The random variables X_i , for $i = 1$ to 100, are independent, and $P(X_i = 1) = P(X_i = -1) = \frac{1}{2}$

Find:

- (i) $Var(X_1)$
- (ii) $Var(X_1 + X_2 + \dots + X_{100})$
- (iii) $Var(100X_1)$
- (iv) $Var(X_1 - X_2)$

Q3 [Practice/E]

- (i) Show algebraically that $E[aX + b] = aE(X) + b$
- (ii) Show that $Var(X) = E(X^2) - \mu^2$
- (iii) Show that $Var(aX + b) = a^2VarX$

Q4 [Problem/H]

If $X \sim B(n, p)$, prove that $E(X) = np$