

Complex Numbers Q13– Practice/Y1/E (22/5/21)

Are these statements true or false? (Give an explanation, or a counter example, as appropriate.)

- (i) All imaginary numbers are complex numbers.
- (ii) All complex numbers are imaginary numbers.
- (iii) All real numbers are complex numbers.
- (iv) Zero is an imaginary number.
- (v) The imaginary part of a complex number is an imaginary number.
- (vi) All complex numbers are either real numbers or imaginary numbers.
- (vii) Two imaginary numbers added together can sometimes give a real number.
- (viii) If two complex numbers multiply to give a real number, then they must be conjugates of each other.
- (ix) The square root of a non-real complex number is never real.

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Solution

(i) True: An imaginary number is a number of the form bi , where b is real; a complex number is a number of the form $a + bi$, where a & b are real, and a can equal zero. Note: "imaginary" numbers are often referred to as "pure imaginary" numbers, to avoid confusion.

(ii) False: The complex number $a + bi$, where $a \neq 0$ is not imaginary, by the definition in (i).

(iii) True: $a + 0i$ is complex.

(iv) True: $0 = 0i$ is imaginary

(v) False: The imaginary part of $a + bi$ is b (not bi : there is an error to this effect in the AQA FP2 website booklet - unless it's been corrected)

(vi) False: $2 + 3i$ is neither real nor imaginary.

(vii) True: For example, i & $-i$

(viii) False: For example, i & i

(ix) True: Suppose that $\sqrt{a + bi} = c$, where $a, b \neq 0$ & c are real; then $a + bi = c^2$, and equating imaginary parts $\Rightarrow b = 0$, which is a contradiction